

1 **Mechanism of secondary eyewall formation in tropical**
2 **cyclones revealed by sensitivity experiments on the mesoscale**
3 **descending inflow**

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15
16 **Abstract**

17 An eyewall replacement cycle is often seen in tropical cyclones, when a secondary
18 eyewall forms outside the inner eyewall, and the inner eyewall disappears. Although this
19 cycle significantly affects the intensity of tropical cyclones, the mechanisms of secondary
20 eyewall formation (SEF) are unclear. Some studies have suggested that dry air inflow and
21 diabatic cooling may have an important role in SEF via the mesoscale descending inflow
22 (MDI). Here, we use numerical experiments to investigate the role of the middle and

1 upper tropospheric dry inflow in SEF. Idealized experiments were conducted using the
2 plane version of the nonhydrostatic icosahedral atmospheric model. Control experiments
3 produced SEF with a dry air inflow in the middle and upper troposphere and associated
4 MDI. In sensitivity experiments, in which the water vapor in the middle and upper
5 troposphere was increased in the outer areas of the tropical cyclone, SEF was hindered
6 and slowed down. These results reveal the role of the dry inflow and associated MDI in
7 SEF.

8

9 **1. Introduction**

10 Eyewall replacement occurs when a secondary eyewall forms outside the inner eyewall
11 of a tropical cyclone (TC), and the inner eyewall disappears. Although many studies have
12 investigated concentric eyewalls and eyewall replacement cycles, there is still no
13 consensus on the mechanism of secondary eyewall formation (SEF). Proposed
14 mechanisms include axisymmetrization of vorticity anomalies (Terwey and Montgomery
15 2008), frictional upwelling due to localized increases in vorticity gradients (Kepert 2013),
16 boundary-layer non-equilibrium dynamics (Huang et al. 2012), and lower-level heating
17 of rainbands (Zhu and Zhu 2014). Huang et al. (2012) also highlight the importance of
18 a gradient wind in the boundary layer. In the boundary layer, angular momentum is
19 transported inward of the TC by the inflow. The tangential wind speed increases when the
20 inflow is enhanced, and the tendency due to angular momentum transport becomes larger
21 than the frictional damping.

22 Recent studies have pointed to the role of the mid-troposphere inflow in SEF. Didlake
23 et al. (2018) show that the mesoscale descending inflow (MDI) contributes to convective

1 enhancement and angular momentum transport in the SEF region. MDI is formed by
2 diabatic cooling in stratiform precipitation regions (Didlake and Houze 2013). Kanada
3 and Nishii (2023) use an observational study to suggest the importance of MDI in SEF.
4 Ge (2015) investigated the effect of the water vapor field around typhoons on SEF,
5 concluding that higher water vapor content favors SEF, which they attribute to the
6 enhanced convective activity associated with the moistening of the atmosphere. However,
7 Ge (2015) did not address the role of the water vapor field in the middle and upper
8 troposphere in SEF. The detailed processes by which the middle and upper inflow
9 influences SEF are not well understood.

10 In this study, we investigate the role of the dry air inflow and MDI using sensitivity
11 experiments in an idealized setting. The paper is organized as follows. Section 2 presents
12 the methodology, and Section 3 presents the results. Section 4 examines the mechanism
13 of SEF by comparing the results with sensitivity experiments in which the amount of
14 water vapor outside a TC varies. Section 5 provides a summary and a discussion of future
15 considerations.

16

17 **2. Methods**

18 We used the plane version of the Nonhydrostatic ICosahedral Atmospheric Model
19 (NICAM; Tomita and Satoh 2004; Satoh et al. 2008, 2014) to conduct an idealized
20 experiment of a TC over the f-plane. NICAM is a global model composed of an
21 icosahedral grid system, but in this experiment, we used a setup called plane-NICAM
22 (Ohno and Satoh 2015; Satoh et al. 2014) in which a rhombic region corresponding to the
23 two adjacent faces of the icosahedron is placed on a plane. When the periodic boundary

1 condition is imposed, this rhombic region is equivalent to a regular hexagonal region. In
2 this study, we performed calculations for a rhombus of 4096 km per side, corresponding
3 to a regular hexagon of 2365 km per side, with a horizontal grid spacing of 2 km, 74
4 vertical layers, and Coriolis parameters fixed at 20°N.

5 We used the Mellor-Yamada-Nakanishi-Niino scheme (Level 2) (Nakanishi, 2001;
6 Nakanishi and Niino, 2004, 2006) for the boundary layer scheme, the NICAM Single-
7 moment Water 6 model (NSW6; Tomita 2008; Roh and Satoh 2014) for the cloud
8 microphysics scheme, and no convection scheme.

9 The vertical profiles of uniform horizontal temperature, pressure, and relative
10 humidity were averaged from a one-month radiative-convective equilibrium experiment.
11 In addition, an initial vortex was placed at the center of the domain. The shape of the
12 initial vortex follows Rotunno and Emanuel (1987), and the parameters follow Wang et
13 al. (2019); the vortex radius is 1000 km, the radius of maximum wind is 80 km, and the
14 maximum wind speed is 25 m s⁻¹. Experiments in which no changes were made to the
15 restart file were considered the control experiment (CTL).

16 After 108 h of integration of CTL, the sensitivity experiment was conducted by
17 changing the water vapor mixing ratio outside the regular hexagonal region, which was
18 centered on the center of the calculation domain. The inner domain, where the vapor
19 mixing ratio was kept unchanged, is inside a regular hexagonal region with sides of length
20 384 km. We conducted two sensitivity experiments: one in which the water vapor mixing
21 ratio was increased by 1.1 (qv1.1) between 6.0 km and 10.0 km in altitude and one in
22 which it was increased by 1.2 (qv1.2). After changing the water vapor mixing ratio, the
23 integration was performed for an additional 60 h.

3. Experiments and results

3.1. Control experiment (CTL)

Figure 1 shows the 1-h accumulated precipitation distribution at an integration time of 114 h to 144 h from the initial condition. (Hereafter, all integration times refer to the hours after the initial condition. At 114 h, eyewall clouds with precipitation of 40 mm or more are produced around the TC at a distance of 50 km from the center. Outside the eyewall, rainband precipitation areas are located around 200 km to 300 km from the TC center. At 120 h, rainband precipitation intensifies around the TC at a radius of 200 km. At 132 h, the precipitation area becomes axisymmetric at a radius of around 150 km, and an outer eyewall forms. At 144 h, the inner wall cloud almost completely disappears, indicating that the eyewall replacement has been achieved.

From this point forth, we focus mainly on the axisymmetric field. The radius-time cross-section of precipitation (Fig. 2(a)) shows the characteristics of the eyewall replacement: precipitation begins to intensify around the TC center at a radius of 300 km at 108 h. This precipitation intensifies and moves inward over time; from about 126 h, it intensifies rapidly and develops into the outer eyewall. At 144 h, precipitation at a radius of around 50 km weakens rapidly, and the inner eyewall disappears. The radius-time cross-section of the ground tangential wind speed (Fig. 2(b)) shows the same characteristics as the precipitation. At around 132 h, the radius of maximum tangential wind increases from the radius of the inner eyewall to that of the outer eyewall (Fig. 2(b)). Then, the outer eyewall gradually moves toward the TC center. Figure 2(c) shows time sequences of the maximum tangential wind and its radius. The speed of the maximum tangential wind decreases from around 100 h until 132 h and then increases. At that time, the radius of the maximum tangential wind jumps from about 50 km to about 130 km;

1 this indicates the eyewall replacement.

2 Next, we investigate the cross-section of the axisymmetric mean wind field at 114 h.

3 At this time, the outer eyewalls are forming, which is considered representative of SEF.

4 Fig. 3(a) shows that tangential wind reaches a maximum at a radius of around 50 km in

5 the lower troposphere. This radius corresponds to the inner eyewall. In addition, a region

6 of tangential wind speed greater than 35 m s^{-1} stretches from a radius of 350 km in the

7 lower atmosphere to a radius of 250 km at an altitude of 8 km. This region corresponds

8 to the inflow from the middle and upper troposphere in the radial wind field (Fig. 3(b)).

9 Fig. 3(b) shows a strong inflow in the lowest layer of the atmosphere and a strong outflow

10 above an altitude of about 10 km. There is also an inflow at an altitude of around 8 km

11 below the outflow at a radius of 250 km to 500 km. The inflow decreases as it approaches

12 the center of the TC and weakens as it reaches a radius of 250 km. Such a flow from the

13 middle to the lower troposphere is considered MDI (Didlake et al. 2018). The vertical

14 wind field (Fig. 3(c)) shows an updraft at a radius of around 50 km, corresponding to that

15 of the inner eyewall, and an upwelling at radii of around 150 km to 200 km, leading to

16 the formation of the outer eyewall. Outside of that, at a radius from 300 km to 500 km,

17 there is a downdraft in the region corresponding to the inflow in the middle and upper

18 troposphere (Fig. 3(b)). The humidity field (Fig. 3(d)) shows dry air intruded in the middle

19 troposphere in the radius from 500 km up to around 300 km, corresponding to the mid-

20 tropospheric inflow (Fig. 3(b)).

21 Figure 3(e) shows the gradient wind component, calculated from the output of

22 instantaneous values every 10 minutes and averaged over 3 h. In the middle layer at a

23 radius of 400 km to 500 km at an altitude of 8 km, the negative values are distributed

24 where the inflow exists, consistent with Wang et al. (2020). In the lower layer at a radius

1 of 150 km to 250 km, as the tangential wind strengthens, a force acts to weaken the inflow
 2 due to the off-axis wind component $\bar{v} \left(f + \frac{\bar{v}}{r} \right) - \frac{1}{\rho} \frac{\partial \bar{p}}{\partial r}$, where \bar{v} represents an azimuthal
 3 mean. This force causes convergence and induces convection outside the original eyewall,
 4 leading to SEF outside the inner eyewall. The induction of convection for the secondary
 5 eyewall as a result of such boundary layer non-equilibrium dynamics has been suggested
 6 by Huang et al. (2012).

7

8 **3.2 Sensitivity experiments**

9 To investigate the effect of water vapor outside the TC, we conducted the sensitivity
 10 experiments qv1.1 and qc1.2, as described in Section 2. The radius-time Hovmöller
 11 diagram of precipitation shows SEF in both sensitivity experiments (Fig. 4). However,
 12 SEF tends to occur later in these experiments than in CTL, as water vapor outside the TC
 13 increases, indicating that this more water vapor condition is unfavorable for SEF. In
 14 addition, the precipitation area corresponding to the outer eyewall extends farther outward
 15 as water vapor content increases. A similar feature is seen in the radius-time Hovmöller
 16 diagram of the surface tangential wind speed (Fig. 4). By contrast, the precipitation and
 17 tangential wind speeds at a radius of around 50 km show that the inner eyewall remains
 18 strong until a later time, as the water vapor content increases.

19

20 **4. The mechanism**

21 Next, we analyzed why the water vapor in the mid-upper troposphere outside the TC
 22 affects SEF. Here, we compare the results of qv1.2 with those of the control experiment.

1 The sensitivity of $qv1.1$ is almost the same as that of $qv1.2$ shown below. In particular,
 2 we show the azimuthally averaged radius-height cross-section at 114 h in the region
 3 spanning from the TC center to a radius of 1500 km.

4 Figure 5(a) shows diabatic heating due to cloud microphysics (shading) and density
 5 (contour). The diabatic heating is averaged over 3 h from hourly instantaneous values
 6 from 111 h to 114 h. When the water vapor outside the TC increases, the diabatic heating
 7 becomes more of a heating anomaly compared to CTL in the domain covering altitudes
 8 of 5–8 km and radii of 250–500 km. In this domain, diabatic cooling due to evaporation
 9 or sublimation of clouds occurs in the mid-level dry inflow in CTL. When the induced air
 10 is more humid, the cooling by evaporation or sublimation becomes weakened. The
 11 heating anomaly in diabatic heating causes the air temperature to rise, resulting in a
 12 negative density anomaly. Figure 5(b) shows vertical wind (shading) and pressure
 13 (contour). The vertical wind becomes more positive in the domain spanning altitudes of
 14 5–8 km and radii 250–500 km, where downdrafts are observed in CTL. This domain
 15 corresponds to the positive density anomalies (Fig. 5(a)), which cause weaker downdrafts
 16 (i.e., the updraft anomalies) than in CTL, as shown in Fig. 5(b). Figure 5(c) shows the
 17 pressure gradient force $-\frac{1}{\rho} \frac{\partial \bar{p}}{\partial r}$ (shading) and the pressure (contour). The pressure
 18 gradient force is a 3-h average of instantaneous values every 10 minutes from 111 h to
 19 114 h. In Fig. 5(c), a low-pressure anomaly occurs around an altitude of 5 km below the
 20 updraft anomaly, and a high-pressure anomaly occurs around an altitude of 11 km above
 21 the updraft anomaly. The pressure gradient force is positive outside of the maximum of
 22 the high-pressure anomaly at an altitude of 11 km and radii between 500 and 1000 km. In
 23 this domain, the inward pressure gradient force becomes smaller than that in CTL. The

1 smaller pressure gradient force weakens the mid-level inflow more than in CTL, as shown
 2 in Fig. 5(d).

3 We next examine the angular momentum budget, which is represented by the
 4 equation

$$5 \frac{\partial \bar{M}}{\partial t} = -\bar{u} \frac{\partial \bar{M}}{\partial r} - \overline{u' \frac{\partial M'}{\partial r}} - \bar{w} \frac{\partial \bar{M}}{\partial z} - \overline{w' \frac{\partial M'}{\partial z}} - \frac{\overline{v' \frac{\partial M'}{\partial \lambda}}}{r} - \frac{\overline{1 \frac{\partial p'}{\partial \lambda}}}{\rho} + r \bar{F}_v,$$

6 where t , r , λ , and z represent time, radius, azimuth, and altitude, respectively; u , v ,

7 w , ρ , and p represent radial wind, tangential wind, vertical wind, density, and pressure,

8 respectively; $M = rv + \frac{1}{2}fr^2$ denotes angular momentum where f is the Coriolis

9 parameter; and F_v is the tendency due to a turbulent process. \bar{A} represents the azimuthal

10 mean of variable A , and A' represents the deviation from \bar{A} . Figure 5(d) shows the

11 inward transport of angular momentum. This is the 3-h average of the instantaneous

12 values every 10 minutes between 111 h and 114 h. The inward transport of angular

13 momentum is smaller than in CTL in the domain around altitudes of 4–8 km and radii

14 250–400 km, where the inflow becomes weaker than in CTL. This results in tangential

15 winds in the middle and upper troposphere being weaker than in CTL, as shown by Fig.

16 5(f).

17 Next, we examine the response in the lower troposphere to the changes in water vapor

18 outside the TC. We show the response at 126 h, which is later than the analysis shown in

19 Fig. 5, when the SEF starts at a radius of around 150 km from the center of the TC. Figure

20 6(a) shows the sum of Coriolis and centrifugal forces $\bar{v} \left(f + \frac{\bar{v}}{r} \right)$ for the 3-h average of

21 instantaneous values every 10 minutes from 123 h to 126 h. It is negatively distributed in

22 the region comprising radii 100–250 km. The difference in the tangential wind between

23 CTL and qv1.2 (Fig. 6(b)) has almost the same distribution as the sum of Coriolis and

1 centrifugal forces. When the tangential wind is weaker than in CTL, the sum of the forces
2 acts toward increasing inflow. It increases with decreasing radius and is particularly large
3 at a radius of around 150 km, which is the SEF area in CTL. When the force acts to
4 strengthen the inflow, a divergence anomaly is generated (contours in Fig. 6(c)).
5 Downdraft anomalies also respond to divergence anomalies (shading in Fig. 6(c)). The
6 tangential wind speed increases when the angular momentum transport due to inflow
7 overcomes the frictional deceleration, and the resulting agradient wind component acts to
8 weaken the boundary layer inflow. The increased tangential wind speed leads to
9 convergence in the SEF region and induces convection.

10 SEF is weakened in these sensitivity experiments in which the amount of water is
11 increased outside the TC, schematically shown in Fig. 7. The upper-level process is
12 related to the change in MDI (Didlake et al. 2018), while the lower-level process is the
13 boundary layer non-equilibrium dynamics (Huang et al. 2012).

15 **5. Conclusions**

16 This study used idealized numerical experiments to investigate the effects of dry air
17 inflow and cooling by evaporation and sublimation in the middle and upper troposphere
18 on SEF. Experiments were conducted using NICAM on an f-plane over a constant sea
19 surface temperature. CTL reproduces SEF and the eyewall replacement cycle. The
20 analysis of CTL reveals dry air inflow in the middle and upper troposphere and the
21 formation of downdrafts due to diabatic cooling. SEF is induced by agradient tangential
22 winds caused by the angular momentum transports due to MDI.

23 To investigate the proposed mechanism, we conducted two experiments in which the

1 amount of water vapor in the middle and upper troposphere outside the TC is increased
2 just before SEF. These experiments showed that SEF is delayed and less favorable. In
3 these experiments, evaporation and sublimation cooling in the inflow region weaken, and
4 this change in diabatic cooling leads to updraft anomalies and weaker inflow in the middle
5 of the troposphere, which are associated with lower and higher pressure anomalies below
6 and above the updraft anomaly, respectively, and a smaller inward pressure gradient in
7 the middle troposphere. The tendency due to the angular momentum transport becomes
8 smaller because of the weakening of the inflow, and the tangential wind also weakens.

9 The weakening of tangential wind in the middle troposphere extends to the lower
10 troposphere. As tangential wind weakens, the agradient wind component acts to
11 strengthen the inflow. The force that strengthens the inflow causes divergence anomalies
12 and weakens convection in the region of SEF.

13 The present study clarifies the mechanism of SEF using an idealized experiment. We
14 analyzed the numerical results and confirmed that the mechanism involves MDI (Didlake
15 and Houze 2013; Didlake et al. 2018) and the boundary layer non-equilibrium dynamics
16 (Huang et al. 2012). Consequently, we will investigate sensitivities to water vapor outside
17 TCs in realistic cases. Our preliminary results confirm that varying the water vapor in the
18 initial field affects the formation of SEF. The results of the present study indicate that
19 better forecasts of TC structures and intensities require more detailed observations of the
20 water vapor field around TCs.

21

22 **Acknowledgments**

23 The numerical simulations were conducted using the FUJITSU Supercomputer

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4 Program, “International Core-to-Core Project on Global Storm Resolving Analysis”.

5

6 **Declaration**

7 The authors have no conflicts of interest to declare.

8

9 **Author contributions**

10 K. K. and M. S. designed this study. K. K. conducted the simulations and analyzed the data
11 of this study. K. K wrote the manuscript. M. S. edited and both approved the manuscript.

12

13 **Data Availability Statement**

14 The numerical experimental data are provided by requests to the authors.

15

16 **Keywords**

17 tropical cyclone, secondary eyewall formation, eyewall replacement cyclone, mesoscale
18 descending inflow

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24

25 **List of Figure Captions**

26 Figure 1. Distribution of 1-h accumulated precipitation [mm] at (a) 114 h, (b) 120 h, (c)
27 126 h, (d) 132 h, (e) 138 h, and (f) 144 h.

28

29 Figure 2. Radius-time cross-section of azimuthally averaged precipitation [mm] (a) and
30 tangential surface wind [m s^{-1}] (b). Time series of maximum tangential wind (red

1 line) and radius of maximum tangential wind (blue line) at surface (c).

2

3 Figure 3. Radius-height cross-section of azimuthally averaged (a) tangential wind [m s^{-1}],
4 (b) radial wind [m s^{-1}], (c) vertical wind [m s^{-1}], (d) relative humidity, and (e)
5 agradient force [$\text{m s}^{-1} \text{ h}^{-1}$].

6

7 Figure 4. Radius-time cross-section of azimuthally averaged (top) precipitation [mm] and
8 (bottom) tangential surface wind [m s^{-1}]. (a) and (d), CTL; (b) and (e), the qv1.1
9 experiment; and (c) and (f), the qv1.2 experiment.

10

11 Figure 5. Difference between CTL and qv1.2 in the axisymmetric radius-height cross-
12 section at 114 h (qv1.2 – CTL). (a) diabatic heating rate [K h^{-1}] (3-h average every
13 1 h) and density [g m^{-3}], (b) vertical wind [m s^{-1}] and pressure [Pa], (c) mean
14 horizontal transport of angular momentum budget [$10^5 \text{ m}^2 \text{ s}^{-1} \text{ h}^{-1}$] (3-h average every
15 10 minutes), (d) radial wind [m s^{-1}], (e) pressure [Pa] and pressure gradient force [m
16 $\text{s}^{-1} \text{ h}^{-1}$] (3-h average every 10 minutes), and (f) tangential wind [m s^{-1}].

17

18 Figure 6. The same as Fig. 5 but for (a) the sum of Coriolis force and centrifugal force
19 $\bar{v} \left(f + \frac{\bar{v}}{r} \right)$ [$\text{m s}^{-1} \text{ h}^{-1}$], (b) tangential wind [m s^{-1}], and (c) vertical wind [m s^{-1}] and
20 the divergence [s^{-1}].

21

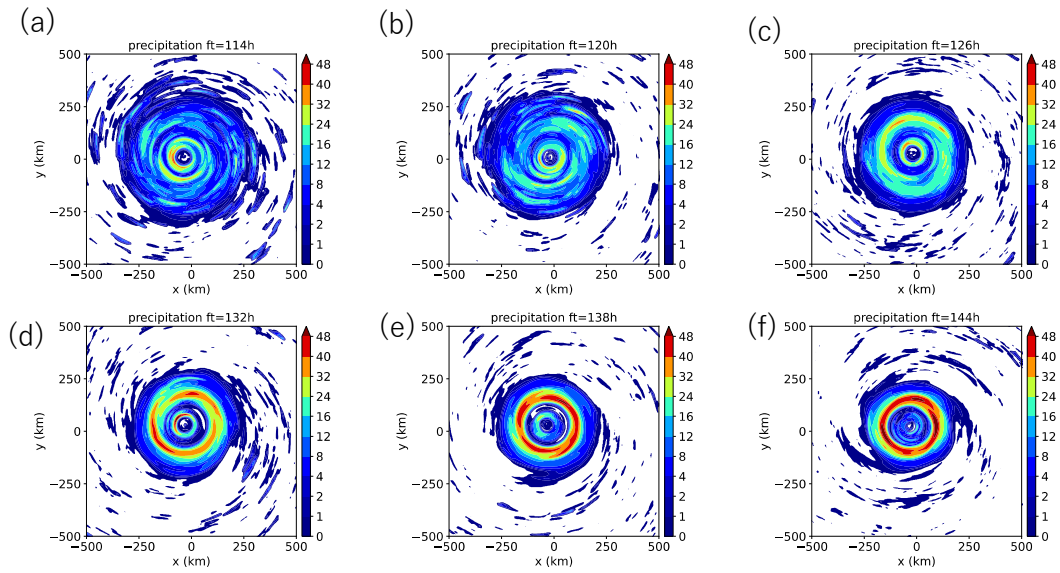
22 Figure 7. Schematic diagrams of the response of the sensitivity experiment in which the
23 amount of water vapor outside the TC is increased: (a) the upper-level process and
24 (b) the lower-level process. In (a), the reduced evaporation or sublimation of water

1 vapor reduces the downward motion of MDI (1), which is associated with the high-
2 and low-pressure responses above and below the upward response region,
3 respectively, (2), and then the mid-level inflow is reduced (3). The reduced MDI
4 leads to the weakening of tangential wind in the region indicated by (4) (and (1) in
5 (b)). In (b), the smaller tangential wind speed (1) enhances the lower inflow at the
6 bottom of MDI (2) and reduces the convergence in the outer eyewall region (3).

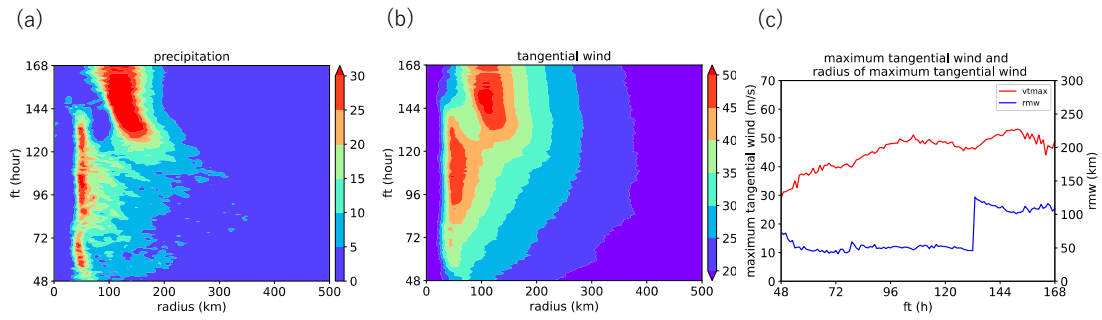
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4



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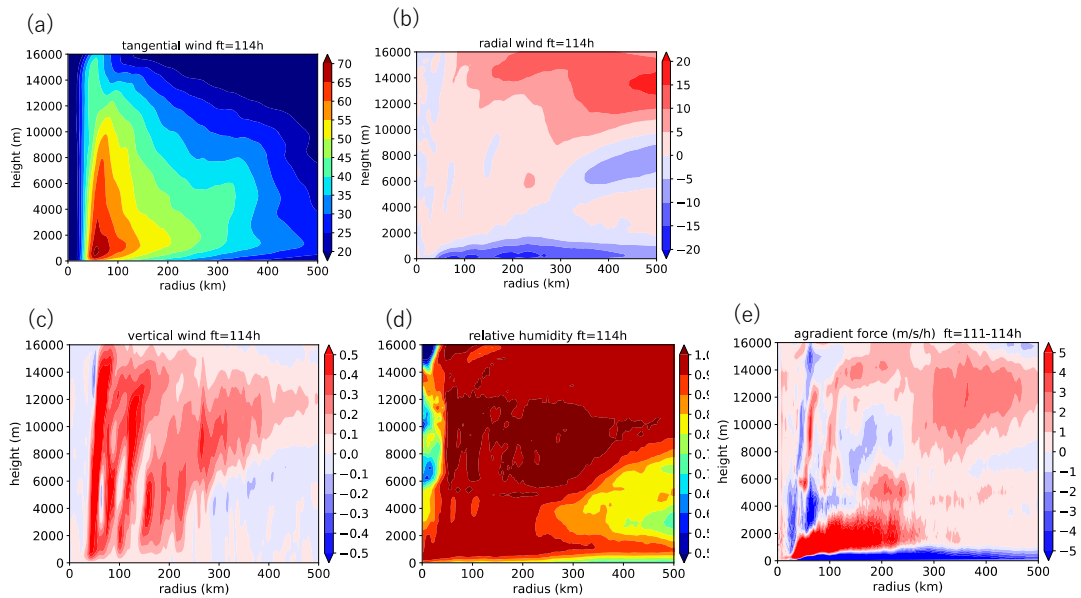
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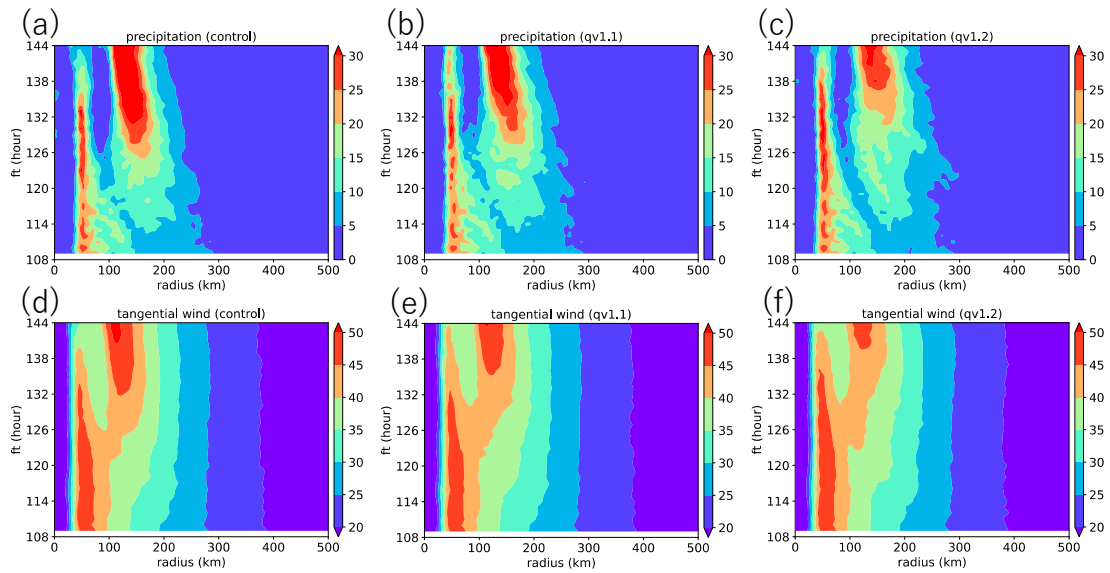
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1 Figure 3. Radius-height cross-section of azimuthally averaged (a) tangential wind [m s^{-1}],
 2 (b) radial wind [m s^{-1}], (c) vertical wind [m s^{-1}], (d) relative humidity, and (c)
 3 agradiant force [$\text{m s}^{-1} \text{ h}^{-1}$].

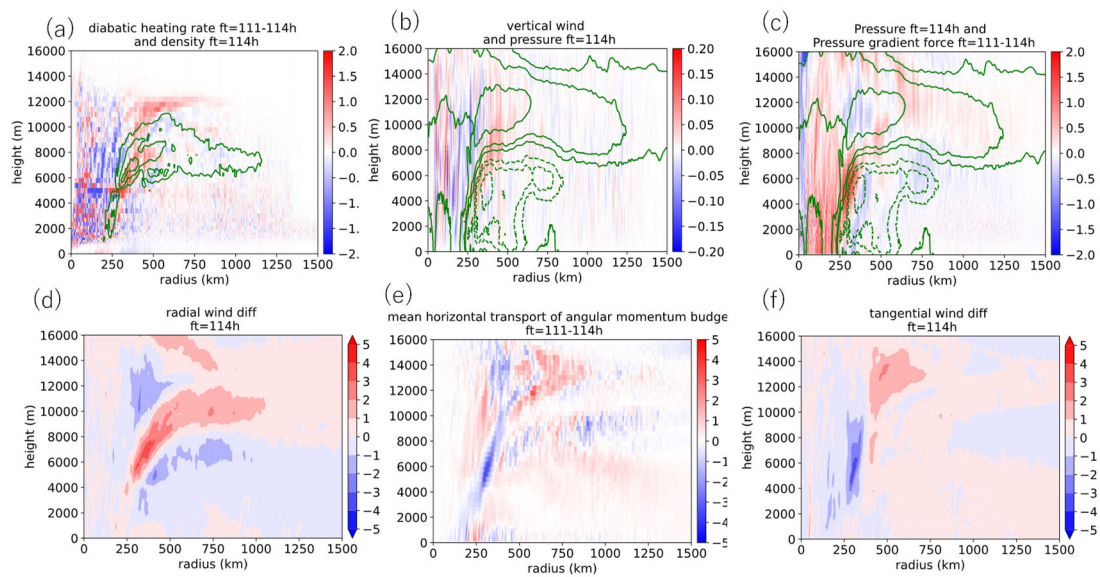


1 Figure 4. Radius-time cross-section of azimuthally averaged (top) precipitation [mm] and
 2 (bottom) tangential surface wind [m s^{-1}]. (a) and (d), CTL; (b) and (e), the qv1.1
 3 experiment; and (c) and (f), the qv1.2 experiment.



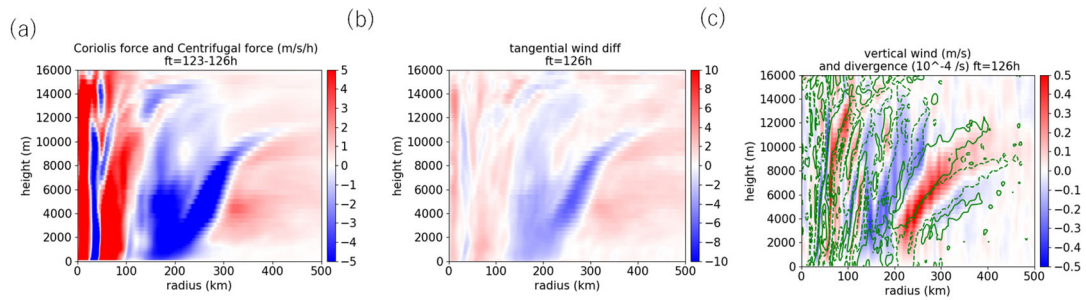
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1 Figure 5. Difference between CTL and qv1.2 in the axisymmetric radius-height cross-
 2 section at 114 h (qv1.2 – CTL). (a) diabatic heating rate [K h^{-1}] (3-h average every
 3 1 h) and density [g m^{-3}], (b) vertical wind [m s^{-1}] and pressure [Pa], (c) mean
 4 horizontal transport of angular momentum budget [$10^5 \text{ m}^2 \text{ s}^{-1} \text{ h}^{-1}$] (3-h average every
 5 10 minutes), (d) radial wind [m s^{-1}], (e) pressure [Pa] and pressure gradient force [m
 6 $\text{s}^{-1} \text{ h}^{-1}$] (3-h average every 10 minutes), and (f) tangential wind [m s^{-1}].



1 Figure 6. The same as Fig. 5 but for (a) the sum of Coriolis force and centrifugal force
 2 $\bar{v} \left(f + \frac{\bar{v}}{r} \right)$ [$\text{m s}^{-1} \text{h}^{-1}$], (b) tangential wind [m s^{-1}], and (c) vertical wind [m s^{-1}] and
 3 the divergence [s^{-1}].

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1 Figure 7. Schematic diagrams of the response of the sensitivity experiment in which the
 2 amount of water vapor outside the TC is increased: (a) the upper-level process and
 3 (b) the lower-level process. In (a), the reduced evaporation or sublimation of water
 4 vapor reduces the downward motion of MDI (1), which is associated with the high-
 5 and low-pressure responses above and below the upward response region,
 6 respectively, (2), and then the mid-level inflow is reduced (3). The reduced MDI
 7 leads to the weakening of tangential wind in the region indicated by (4) (and (1) in
 8 (b)). In (b), the smaller tangential wind speed (1) enhances the lower inflow at the
 9 bottom of MDI (2) and reduces the convergence in the outer eyewall region (3).

